

Discharge Modeling in Smooth and Rough Compound Channels Using Genetic Programming

[Alok Adhikari¹, N Adhikari,² and K C Patra³]

Abstract— Discharge results observed from the experimental channels for smooth and rough surfaces, along with data from a compound river channel are used in the Genetic Programming. Model equations are derived for prediction of discharge in compound channel for various types of channel surfaces. Five hydraulic parameters are used for developing the model equations. Models derived are tested and compared with other soft computing techniques. Evaluations of all the approaches are carried out using five performance parameters. Finally, the effect of parameters responsible for the flow behavior is shown through sensitivity analysis. GP is found to give the most promising results. This work aims to benefit the researchers engaged in modeling of discharge using machine learning techniques.

Keywords— cnn, fuzzy, ces, anfis, gp

I. Introduction

In hydrology a reliable assessment for discharge of a compound river section encompassing a deep main along with floodplains are subject of extensive research. The quantum of flow is very complex. The prediction of same helps in overall design, operation and maintenance of streams and its periphery. The overall conveyance of the compound channels is a function of stage and various other parameters like the hydraulics radius, cross sectional area, wetted perimeter, bed slope, roughness, shear, depth ratio, width ratio, sinuosity, viscosity, gravitational acceleration, momentum transfer mechanism etc. The detail literature study reveals that very limited works have been made where laboratory data collected in controlled environment are used for prediction. Mohanty et al. [1] used laboratory data for developing flow equations and tried to use them to compare with the flow behavior of river Batu [2] using a conventional method. Though the soft computing models like Artificial Neural Network (ANN) and Adaptive Neuro Fuzzy Inference System (ANFIS) are used for prediction of discharge but derivation of a model equation is very complex. During prediction, ANN modeling reduces the tedious effort of experimentation and complexity in computation [3 & 4]. In case there is shortage of data due to any error or physical phenomena then synthetic data can be reconstructed [5]. The models with artificial intelligence do not explicitly follow physical principles inside a system [6]. They constitute a universal approximation of the input and output and have the capability to reconstruct missing data. While among ANN modelling approaches Back Propagation Network (BPN) and CASCADE equations are established for input parameter (Stage) and output (Discharge), but are more complex [7 & 8]. In ANFIS the presence of multiple parameters as inputs, makes it difficult to derive model equations [9].

To study and analyze the flow behavior, experimental channel is set up. Laboratory experimental data of Flood Channel Facility, Wallingford England are available globally [10-13] and are included in the data set. Apart from experimental data, the actual river data is used to build the data set. The current work analyses river data along with the laboratory data to get a generalized solution to the above problems. Impacts of the hydraulic parameters to the flow behavior need to be studied. To

overcome this, attempts have been made to study and apply the Genetic Programming (GP) [14-16]. Due to a forced restriction on GP tree depth, the evolved mathematical models are compact. Hence the influence of input parameters is easy to study.

II. Experimental Arrangement

Experiments are conducted in a straight compound channel with symmetrical flood plains in a flume of dimensions measuring 12m×2m×0.6m in the Hydraulics Engineering laboratory of the National Institute of Technology Rourkela, India. Fabrication of channel is made with Perspex sheet of 0.006 meter having a uniform Manning's n value of 0.01. The compound channel has the width ratio (α) as 15.75 and the aspect ratio (δ) of trapezoidal main channel is 1.5. the details of experimental channel shown in Fig.1 can be found in our earlier work [9]. The experimental channel section is shown in Fig.2 and the photographs for the entire set up are shown in Fig. 3(a-h).

In order to study the effect of roughness on the flow behavior during high floods experiments were carried out in different runs. First one was with plane surface and next three runs were carried out with different roughening materials to provide the effect of vegetation [9].

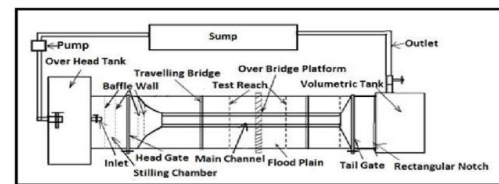


Figure 1. Schematic drawing of whole experimental tilting flume

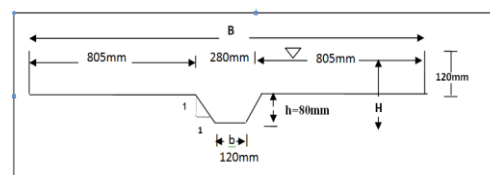


Figure 2. Straight Compound Channel Section



Figure 3. Photographs of whole experimental system

III. Data Collection

In the current work, present experimental set up data is combined with other researcher's data [10-13]. Then actual river data is also collected from two gauging stations

¹Research Scholar, Department of Civil Engineering, NIT Rourkela, India,

²Biju Patnaik University of Technology, Rourkela, India and

³Professor, Department of Civil Engineering, NIT Rourkela, India.

namely Panposh and Gomlai in Sundergarh district of Odisha state for River Bramhani. Data sets observed from these sets of experimental channels (smooth channel = data set I, rough channel = data set II, smooth + rough = data set III, river data = data set IV and combination of all above mentioned data sets taken as data set V) are grouped and named as they are used in the analysis. Five different channel parameters that are affecting stage discharge relations are selected for the analysis [1]. These parameters are: (1) Width ratio α , (2) roughness coefficient of flood plain n_{fp} , (3) bed slope S_0 , (4) relative depth of flood plane to total depth β and (5) hydraulic radius R_T .

IV. Artificial Intelligence Techniques

Artificial Intelligence (AI) techniques are the best alternative to classical techniques to model environmental systems. AI techniques can be case-based reasoning, rule-based systems, ANNs, Fuzzy Inference models, genetic algorithms, cellular automata, multi-agent systems, swarm intelligence and hybrid systems etc. ANN is a very vigorous technique to develop immense relationship between input and output variables. Using various types of ANN such as Back Propagation Network, Cascade, Radial Basis Function (RBF), and Elman Neural Network, discharge predictions are carried out for the corresponding stages and reported in our previous works [7 & 8]. Similarly Fuzzy logic developed by Zadeh is used successfully for prediction of discharge. ANFIS is a very popular technique and is used by many researchers [17 & 18]. The same has been used by our earlier reported work [9]. In the current study, emphasis is given to another robust tool, Genetic Programming- a multi gene symbolic regression technique.

V. Genetic Programming

Genetic programming (GP) is an optimization tool motivated from general biology. It randomly generates a population of computer programs for optimization. Here the computer programs are internally represented as tree structures. Then mutation and crossover is carried out on best performing trees to find a new population. This process is iterated until the population contains the programs that solve the task well. For the current research, the open source MATLAB toolbox called GPTIPS is used as it is developed for specific purpose of performing symbolic regression. It employs a unique type of symbolic regression called multigene symbolic regression [16] that evolves linear combinations of non linear transformations of the input variables. In standard symbolic regression techniques, the evolved models are not restricted to low orders depending on the supplied data sets. Whereas in GPTIPS the transformation is restricted to be low order (by restricting the GP tree depth) irrespective of the predictor – response (input-output) data sets even when there are a large set of input parameters. A brief overview of the multigene low order GP approach is given in the next section. GP model is composed of nodes, which resembles a tree structure and thus, it is known as GP tree. Nodes are the elements either from a functional set or terminal set. A functional set may include arithmetic operators (+, -, *, /), mathematical functions (sin(.), cos(.), tanh or ln(.)),

Boolean operators (AND, OR, NOT, etc), logical expressions (IF, or THEN) or any other suitable functions defined by the users, whereas the terminal set include variables (like x_1, x_2, x_3 , etc) or constants (like 1,2,3,4 etc.) or both. The functions and terminals are randomly chosen to form a GP tree with a root node and the branches extending from each function node to end in terminal nodes as shown in Fig. 4 for the expression $y = ax_1 + \log bx_2$, a and b being the coefficients.

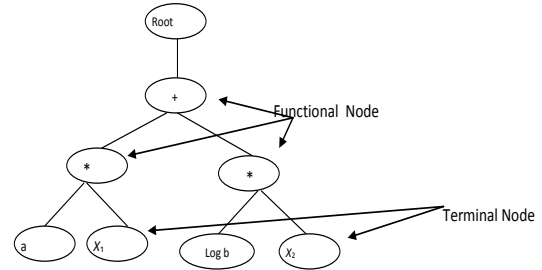


Figure 4. GP Tree for expression $ax_1 + \text{Log } b x_2$

A. Discharge Prediction Using GPTIPS

From previous studies it is observed that different hydraulic parameters play crucial role for discharge carrying capacity in a channel. Using artificial neural networks with stage as single input to predict discharge as the output, different network models are derived. It is observed the model equations derived are very complex. Therefore hydraulic characteristics like bed slope, hydraulic radius, roughness coefficient, aspect ratio, relative depth of compound channel are taken as input for predicting discharge. The generalized model equation is represented as:

$$Q = \sum_{i=1}^n F(X, f(X), b_i) + b_0 \quad (1)$$

where Q stands for Discharge, F is the function created by GP model, X is the vector of input variables $\{\alpha, n_{fp}, S_0, \beta \text{ and } R_T\}$, b_i represents constants, f is user defined function, n is the number of terms of target expression and b_0 is bias.

B. GPTIPS Run Settings

A GPTIPS run settings is performed for all the above data sets. Initially a set of GP trees, as per the data sets of each model are randomly generated using various functions and terminals assigned. The fitness criteria are calculated by the objective function, which determines the quality of each individual competing with the rest of the population. At each generation, a new population is created by implementing various evolutionary mechanisms like reproduction, crossover and mutation of the selected GP trees entering into the mating pool. The new population then replaces the existing population. This process is iterated until the termination criterion, which can be either a threshold fitness value or maximum number of generations is satisfied. The best GP model, based on its fitness value is selected as the result of genetic programming. The default GPTIPS multigene symbolic regression function is used in order to minimize the root mean squared prediction error on the testing data. Table 1 describes the best GP model derived for each data set with population size, number of generations, tournament size, depth of tree and maximum number of genes.

TABLE I. DESCRIPTION OF GP MODELS FOR DIFFERENT DATA

Data Set	Training data (Initial population)	Testing data	No. of Generations	Tournament size	D_{max}	G_{max}	Function Node set
I	120	20	77	4	3	5	+, -, *, /, tanh, plog, square
II	28	10	0	4	4	5	
III	150	28	12	4	3	5	
IV	50	24	48	4	4	5	
V	222	50	206	4	4	5	

VI. Interpretation of Results

In the GP modeling, normalization or scaling of the data is not required as it is done in ANN in the range [-1,1]. For the GP simulations, the population size and the number of generations are equal to the number of inputs as described in Table 1. For selection of parent genes from the pool of available solutions, a tournament selection strategy is adopted with size selected as 4. The maximum depth of each tree is set to 5 to have more control over the evolved equations. The crossover, mutation and direct reproduction probabilities are taken as 0.85, 0.1 and 0.05 respectively.

Here a number of potential models are evolved at random and each model is trained and tested using the training and testing data respectively. The fitness of each model is determined by the RMSE between the predicted and actual value of output that is discharge (Q) as the objective function given as:

$$RMSE = \sqrt{\frac{\sum_{i=1}^n (Q_m - Q_p)^2}{n}} \quad (2)$$

where, n is the number of cases in the fitness group. If the errors calculated by using Eq. 2 for all models in the existing population do not satisfy the termination criteria, the generation of new population continues till the best model is developed as per the earlier discussion. In the GP model development it is important to make a tradeoff between accuracy and complexity in terms of the number of genes and depth of the GP tree. The developed GP model for all the five data sets are described as Eqs (3) to (7) as shown in Table 2.

A. Prediction Using Data Set I

In Fig. 5, first plot shows fitness, second shows prediction and third with bias -0.02085 as shown in Eq. 3) and gene values for smooth data set I. During several runs for smooth data the best fitness is achieved at generation 77 with minimum bias while RMSE for training as 0.020 and testing as 0.392.

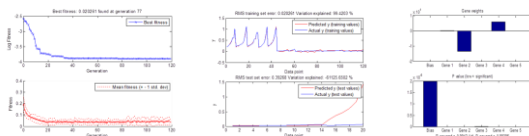


Figure 5. Plot for Fitness, Prediction along with Bias and Gene for Smooth data in GP

B. Prediction Using Data Set II

Fig. 6 shows fitness, prediction along with bias 0.1274 (as in Eq. 3) and gene values for rough data set II.

TABLE II. EQUATIONS DERIVED FOR DIFFERENT GP MODELS

Model	Developed Equation	Eq.No
Model I (Smooth)	$Q = 42.42S_p R_c \alpha^2 + (5.174R_c^2 + 0.9396R_c + 0.7491\beta - 95.41n_p\beta)\alpha - 0.7491\beta + 0.9396\tanh(\beta) - 0.02085$	(3)
Model II (Rough)	$Q = 2.764S_p - 0.0129\alpha - 0.1594\beta + 2.923R_c + 0.07304\text{plog}(3.105) - 3.357\tanh(n_p) + 0.1274$	(4)
Model III (Smooth and Rough)	$Q = 0.0008305n_p - 0.0008305S_p - 0.1078\beta + 0.6329\alpha R_c + 11.27\alpha R_c^2 - 0.0008305\alpha^2 - 206.2\alpha n_p \beta R_c + 0.001579$	(5)
Model IV (River)	$Q = 176.7R_c^2 \tanh(R_c) + 1610.0\beta \tanh(\beta) - 4.535 \times 10^4 S_p \beta (\text{plog}(\beta) + \tanh(\alpha)) + 38.2\text{plog}(\alpha - R_c) \tanh(\beta)(\beta + R_c) - 47.45$	(6)
Model V (Smooth, Rough and River)	$Q = 590.6(n_p + R_c)^2 - 1.137 \times 10^4 n_p^2 R_c - 18700.0R_c^2 (n_p + S_p) + 2.294 \times 10^4 n_p S_p R_c^2 + 6.517 \times 10^4 n_p^2 \beta R_c - 3.052$	(7)

During the several runs for rough data, fitness is achieved with RMSE for training as 0.011 and for testing as 0.002 at generation 0.

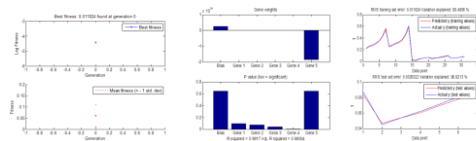


Figure 6. Plot for Fitness, Prediction along with Bias and Gene for Rough data set II in GP

C. Prediction Using Data Set III

Fitness, prediction curve including bias 0.01579 (shown in Eq. 4) and gene for data set III are shown in Fig. 7. Best fitness is achieved for this model at generation 12 with minimum bias along with RMSE training of 0.048 and testing of 0.130.

D. Prediction Using Data Set IV

For River data best fitness is achieved at generation 48 with minimum bias -47.45 shown in Eq. (5) having RMSE for training of 71.718 and testing of 103.4 (Fig. 8).

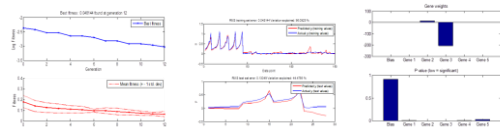


Figure 7. Plot for Fitness, Prediction along with Bias and Gene for Smooth and Rough data in GP

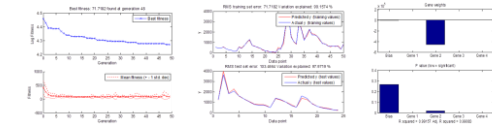


Figure 8. Fitness, Prediction Plot along with Bias and Gene for River data in GP

E. Prediction Using Data Set V

Similarly for data set V, (combination of all data) the best fitness is achieved at generation 206 with minimum bias -3.052 (shown in Eq. 6) having RMSE for training as 21.628 and testing as 16.01 (Figure 9).

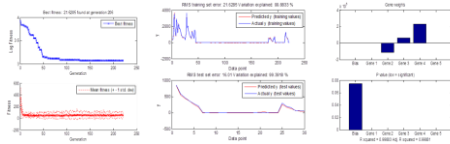


Figure 9. Plot for Fitness, Prediction along with Bias and Gene for data set V in GP

F. Sensitivity Analysis

This is an important aspect of a developed model to find out the relative effect of the input parameters. Different approaches have been suggested by researchers to select the important input variables. In the current study sensitivity analysis is made following Liong et al 2002 for all five data sets in GP. As per Liong, the sensitivity (S_i) of each parameter is determined by varying it while others are kept constant at the same time. It is expressed as,

$$S_i = \frac{1}{N} \sum_i^N \left(\frac{\% \text{Change in output}}{\% \text{Change in input}} \right) \times 100 \quad (8)$$

TABLE III. SENSITIVITY ANALYSIS AND RANKING

PARAMETER	Data Set I		Data Set II		Data Set III		Data Set IV		Data Set V		Rank Index
	Value	R _i	Value	R _i	Value	R _i	Value	R _i	Value	R _i	
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
α	1.467	2	-7.978	1	0.937	5	0	4	0	5	17
N_c	0	4	-3.652	3	-2.810	4	-0.075	3	2.273	2	16
S_o	0	4	-3.226	4	-3.438	3	0	4	0.077	4	19
β	0.009	3	-3.679	2	-3.531	2	0.739	2	-0.457	3	12
R_z	4.303	1	-2.124	5	5.049	1	12.996	1	4.191	1	9

All ranks corresponding to data sets are listed in Table 3 (columns 3, 5, 7, 9, and 11). Column 12 presents sensitivity analysis. As per GP, the hydraulics radius is the most important parameter found in case of all five models with least rank index of 9 followed by β , n_{fp} , α and S_o in order of their ranking index.

G. Comparison of Prediction by Soft Computing Models

This section presents a comparison of prediction done by GP with other soft computing techniques described earlier. The Cascade neural network is not compared here as it has reported to have given very poor performance.

Performances of the models are judged by taking some global statistical parameters for the current analysis of all the models such as; Average Absolute Relative Error (AARE), Normalised Mean Bias Error (NMBE), Pearson's Correlation coefficient (R), Nash-Sutcliff efficiency (E) and Normalized Root Mean Square Error (NRMSE) (e.g. Srinivasulu et al. 2006). More details on these parameters are available in other reported works [7-9].

Performance parameters for GP, ANFIS, Fuzzy and CES are calculated and given in Table 4 for comparison. The results from the soft computing models namely ANFIS and GP are compared. As Fuzzy and CES give higher percentage of errors in their predictions in comparison to ANFIS and GP, they are excluded from the comparison plots for clarity reasons.

TABLE IV. EVALUATION OF PERFORMANCE PARAMETERS AND RANKING FOR ALL MODELS

Data Set	Methods	AARE	R _i	NMBE	R _i	R	R _i	E	R _i	NRMSE	R _i	Rank Index (Sum R _i : R)
		(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)
I	GP	21.041	2	-0.158	2	0.838	3	0.999	1	0.288	1	9
	ANFIS	22.876	3	0.159	3	0.934	1	0.526	3	0.298	2	12
	CES	18.116	1	-0.068	1	0.895	2	0.836	2	0.506	3	9
	FUZZY	57.744	4	1.677	4	0.113	4	-0.955	4	2.028	4	20
II	GP	5.727	1	-0.018	2	0.205	4	1.000	1	0.005	1	9
	ANFIS	20.932	3	0.013	1	0.465	1	0.968	2	0.007	2	9
	CES	14.993	2	-0.901	3	0.464	2	0.345	3	0.936	3	13
	FUZZY	45.745	4	2.724	4	0.314	3	-221.0	4	3.312	4	19
III	GP	37.225	3	0.040	1	0.991	1	0.980	1	0.169	1	7
	ANFIS	26.874	2	-0.162	2	0.972	3	0.954	2	0.255	2	11
	CES	18.001	1	0.168	3	0.992	2	0.920	3	0.336	3	12
	FUZZY	132.73	4	-0.503	4	0.868	4	0.791	4	0.885	4	20
IV	GP	3.016	1	-0.013	2	0.996	2	0.991	2	0.047	2	9
	ANFIS	3.346	2	0.011	1	0.997	1	1.000	1	0.046	1	6
	CES	142.63	4	-0.593	4	0.994	3	-0.827	4	0.664	3	18
	FUZZY	7.014	3	0.023	3	0.986	4	0.968	3	0.088	4	17
V	GP	75.926	3	0.188	3	0.592	4	0.997	1	0.146	1	12
	ANFIS	84.835	4	-0.061	2	0.877	1	0.992	2	0.352	3	12
	CES	42.954	1	-0.512	4	0.872	3	0.660	4	1.067	4	16
	FUZZY	74.026	2	-0.002	1	0.874	2	0.991	3	0.175	2	10

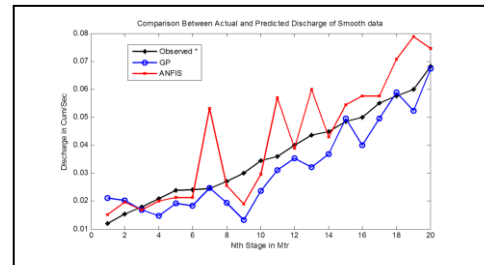


Figure 10. Predicted discharge using GP and ANFIS for Data Set I

The Fig. 11 shows the prediction of discharge by GP and ANFIS along with observed discharge for data set I. ANFIS shows little over prediction while GP makes slightly under prediction. However for all stage values, GP has shown better prediction following the trend of observed data. The ranking of evaluation parameter performance of AARE (column 2), NMBE (column 4), R (column 6), E in column 8 and NRMSE (column 10) are given in Table 5. It can be safely concluded that, whether in individual ranking or in group rank index, GP and CES scores the highest rank (column 11 of Table 5).

Fig. 12 shows the prediction using rough data set II. Prediction by GP is very close to the observed value than ANFIS for all stages. As GP bears lowest AARE (5.7), NMBE (-0.018), E value equal to 1.0, hence it's performance is found to be the best. NRMSE for GP is better (0.005) when compared to ANFIS. The Fig. 13 depicts the plot for smooth and rough data. From Table 5, it is also quite clear that GP and ANFIS give better modelled rank performance than CES and FUZZY.

The Fig. 14 presents prediction plot for data of Brahmani river. As per rank index, GP performs poor than ANFIS but is better than CES and FUZZY. The prediction graphs of Fig. 15 is for the combined data which contains very low as well as very high discharge values of stage in increasing order. Up to 30 test data points its very low as shown in the Figure 15. Beyond 32 to 50, it represents very high magnitude of flow. Rank value got for GP and ANFIS are same but, from the plots it is clear that GP follows the

same trend as that of observed discharge whereas the ANFIS model exhibits bit over prediction.

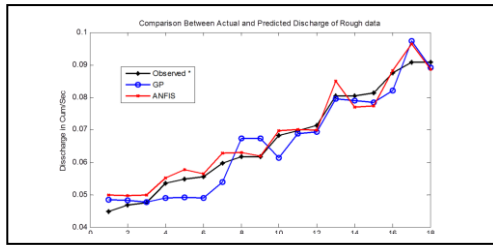


Figure 11. Predicted discharge using GP and ANFIS for Data Set II

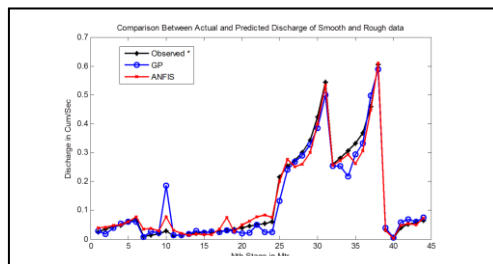


Figure 12. Predicted discharge using GP and ANFIS for Data Set III

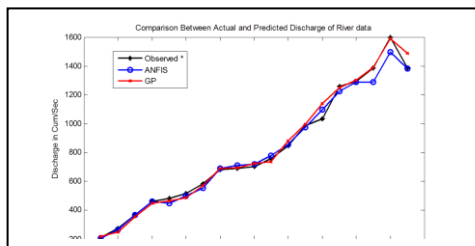


Figure 13. Predicted discharge using GP and ANFIS of Data Set IV

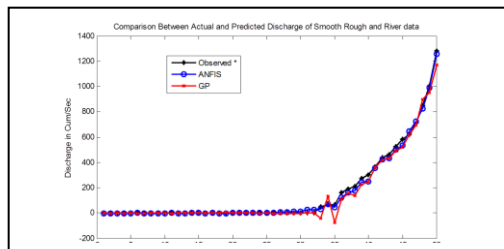


Figure 14. Predicted discharge using GP and Data Set V

The overall performance of models is ranked and final rank index is calculated for each data set with respect to all the ranking criteria. Least value of rank index justifies the goodness of the model. GP rank index varies from 7 to 12 where as ANFIS rank index values vary from 6 to 12 as shown in Table 5. The rank index for CES from 9 to 18 and the same for FUZZY varies from 10 to 20. From final rank index in Table 5 (column 7) it is inferred that GP model exhibits consistent performance for all the five data sets while others show variable performance. Thus, it can be concluded that the Genetic Programming can perform well in predicting a wide range of flow in the river system.

TABLE V. FINAL RANKING OF ALL MODELS

Models	Data Set I	Data Set II	Data Set III	Data Set IV	Data Set V	Rank Index
(1)	(2)	(3)	(4)	(5)	(6)	(7)
GP	9	9	7	9	12	46
ANFIS	12	9	11	6	12	50
CES	9	13	12	18	16	68
FUZZY	20	19	20	17	10	86

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About Author (s):

Alok Adhikari: A research scholar in Department of Water Resources Engineering, National Institute of Technology, Rourkela, India. He has done M.Tech in Soil and Water Conservation Engineering from OUAT, Bhubaneswar, India.

Dr Nibedita Adhikari is attached to Biju Patnaik University of Technology, Odisha, India. Her research area includes Soft Computing and Paralle computing.

Dr K. C. Patra is working as Professor in Department of Civil Engineering , NIT Rourkela, India.