Observer Linearization for Nonlinear Systems Using Piecewise Multi-Linear Model

Tadanari Taniguchi and Michio Sugeno

Abstract— **This paper proposes an observer design for piecewise nonlinear systems via observer linearization. The model is a piecewise multi-linear (PML) system, a nonlinear approximation, and fully parametric. Feedback linearization is applied to stabilize PML control system. However, since exact observer linearized conditions are more conservative than exact feedback linearized ones, the exact observer linearization can be applied to only a few nonlinear systems. This paper shows the PML model based linearized observer can be applied to a wider system than the conventional one. We apply the proposed method to TORA (Translational Oscillator with Rotating Actuator) system which is one of the benchmark problem for nonlinear control. Example is shown to confirm the feasibility of our proposals by computer simulation.**

Keywords—**observer linearization, piecewise multi-linear model, nonlinear control, feedback linearization**

I. Introduction

Piecewise linear (PL) systems which are fully parametric have been intensively studied in connection with nonlinear systems [1], [2], [3], [4]. We are interested in the parametric piecewise approximation of nonlinear control systems based on the original idea of PL approximation. The PL approximation has general approximation capability for nonlinear functions with a given precision.

Sugeno suggested to use the piecewise multi-linear (PML) approximation [5]. PML approximation also has general approximation capability for nonlinear functions with a given precision. We note that a multi-linear function as a basis of PML approximation is, as a nonlinear function, the second simplest one after a linear function. The PML model has the following features. 1) The PML model is derived from fuzzy if-then rules with singleton consequents. 2) It is built on piecewise hyper-cubes partitioned in the state space. 3) It has general approximation capability for nonlinear systems. 4) It is a piecewise nonlinear model, the second simplest after a PL model. 5) It is continuous and fully parametric. The authors of this paper have been researching the PML systems [6-7], [9-12], [15-18].

This paper proposes an observer design for piecewise nonlinear systems via observer linearization. Feedback linearization can be applied to stabilize PML control system. However, since the observer linearized conditions are more conservative than feedback linearized ones the observer linearization can be applied to only a few nonlinear systems.

In comparison with the other observer designs [11], [12], this paper deals with the necessary and sufficient conditions for observer linearization. We show the PML model based linearized observer can be applied to a wider system than the conventional one. We apply the proposed method to TORA system which is one of the benchmark problem for nonlinear control.

This paper is organized as follows. Section II introduces the canonical form of PML models. Sections III and IV briefly present feedback linearization and observer linearization. Sections V and VI represent TORA system and the PML model. Sections VII and VIII propose the controllers and the observers of TORA system. Section IX shows an example demonstrating the feasibility of the proposed methods. Finally, section X summarizes conclusions.

II. Canonical Forms of Piecewise Multi-Linear Models

We introduce PML models suggested in [5]. We deal with the n-dimensional case of a nonlinear control system. Define vector $d(\sigma_1,\ldots,\sigma_n)$ and rectangle $R_{\sigma_1\cdots\sigma_n}$ in n-dimensional space as $d(\sigma_1,\ldots,\sigma_n) \equiv (d_1(\sigma_1),\ldots,d_n(\sigma_n))^T$,

$$R_{\sigma_1\cdots\sigma_n} \equiv [d_1(\sigma_1),d_1(\sigma_1+1)]\times[d_2(\sigma_2),d_2(\sigma_2+1)]$$
$$\cdots\times[d_n(\sigma_n),d_n(\sigma_n+1)],$$

where σ_i is integer: $-\infty < \sigma_i < \infty$, $d_i(\sigma_i) < d_i(\sigma_i+1)$ and $d(0) \equiv (d_1(0),d_2(0),\ldots,d_n(0))^T$. Superscript T denotes a *transpose* operation.

We consider an n-dimensional nonlinear control system.

$$\begin{cases} \dot{x} = f(x) + g(x)u(x) \\ y = h(x) \end{cases} \tag{1}$$

For $x \in R_{\sigma_1\ldots\sigma_n}$, the PML model (2) is constructed from the nonlinear system (1).

$$\begin{cases} \dot{x} = f_p(x) + g_p(x)u(x) \\ y = h_p(x), \end{cases} \tag{2}$$

where

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$$\begin{cases} f_p(x) = \sum_{i_1=\sigma_1}^{\sigma_1+1} \cdots \sum_{i_n=\sigma_n}^{\sigma_n+1} \omega_1^{i_1}(x_1)\cdots\omega_n^{i_n}(x_n) f(i_1,\ldots,i_n), \\[2mm] g_p(x) = \sum_{i_1=\sigma_1}^{\sigma_1+1} \cdots \sum_{i_n=\sigma_n}^{\sigma_n+1} \omega_1^{i_1}(x_1)\cdots\omega_n^{i_n}(x_n) g(i_1,\ldots,i_n), \\[2mm] h_p(x) = \sum_{i_1=\sigma_1}^{\sigma_1+1} \cdots \sum_{i_n=\sigma_n}^{\sigma_n+1} \omega_1^{i_1}(x_1)\cdots\omega_n^{i_n}(x_n) h(i_1,\ldots,i_n), \\[2mm] x = \sum_{i_1=\sigma_1}^{\sigma_1+1} \cdots \sum_{i_n=\sigma_n}^{\sigma_n+1} \omega_1^{i_1}(x_1)\cdots\omega_n^{i_n}(x_n) d(i_1,\ldots,i_n), \end{cases} \quad (3)$$

and $f(i_1,\ldots i_n)$, $g(i_1,\ldots i_n)$, $h(i_1,\ldots i_n)$, and $d(i_1,\ldots i_n)$ are the vertices of the nonlinear system (1). The membership functions are

$$\begin{cases} \omega_j^{\sigma_j}(x_j) = \dfrac{d_j(\sigma_j+1) - x_j}{d_j(\sigma_j+1) - d_j(\sigma_j)}, \\[3mm] \omega_j^{\sigma_j+1}(x_j) = \dfrac{x_j - d_j(\sigma_j)}{d_j(\sigma_j+1) - d_j(\sigma_j)}, \end{cases}$$

$j = 1,\ldots,n$, $\omega_j^i(x_j) \in [0 \quad 1]$, and $x = (x_1,\ldots,x_n)^T$. In the above, we assume $f(0,0) = 0$ and $d(0,0) = 0$ to guarantee $\dot{x} = 0$ for $x = 0$.
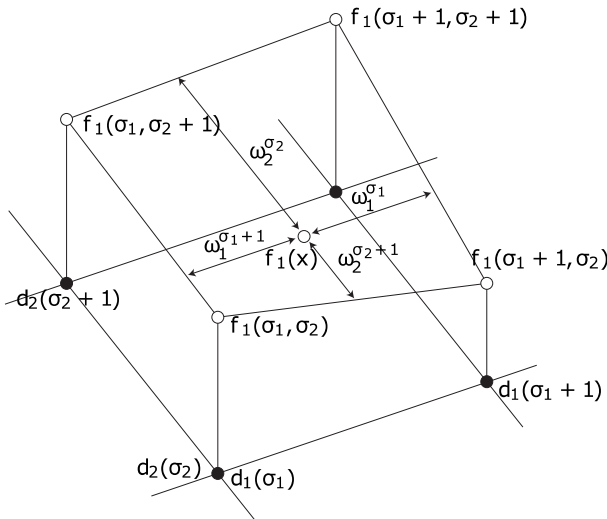

Figure 1: A piecewise region of $f_1(x)$ in 2D case

We explain the modeling procedure of PML system in two-dimensional case.

1) Assign vertices $d(i_1,i_2)$ for $x_1 = d_1(\sigma_1)$, $d_1(\sigma_1+1)$, $x_2 = d_2(\sigma_2)$, $d_2(\sigma_2+1)$ of state vector x, then partition state space into piecewise regions (see Fig. 1).

2) Compute vertices $f(i_1,i_2)$, $g(i_1,i_2)$ and $h(i_1,i_2)$ in equation (3) by substituting values of $x_1 = d_1(\sigma_1)$, $d_1(\sigma_1+1)$ and $x_2 = d_2(\sigma_2)$, $d_2(\sigma_2+1)$ into original nonlinear functions $f(x)$, $g(x)$ and $h(x)$ in the system (1). Fig. 1 shows the expression of $f_1(x)$ and $x \in R_{\sigma_1\sigma_2}$.

The overall PML model is obtained automatically when all vertices are assigned. Note that $f(x)$, $g(x)$ and $h(x)$ in the PML model coincide with those in the original system at vertices of all regions.

III. Feedback Linearization

This section deals with a feedback linearizing controller for PML model. Since the stabilizing conditions are represented by bilinear matrix inequalities (BMIs) [8], it requires a long computing time to obtain a stabilizing controller. To overcome the difficulty, we derived the stabilizing conditions [9], [10] based on feedback linearization approaches.

First we give a brief introduction to the feedback linearization [13] of nonlinear systems. We consider the nonlinear system (1), where $f(x)$, $g(x)$ and $h(x)$ are assumed to be sufficiently smooth in a domain $D \subset R^n$. The mappings $f : D \to R^n$ and $D \to R^n$ are called vector fields on D. The time derivatives of the output y are calculated until the input u appears. Then the controller is obtained as

$$u = (-L_f^\rho h(x) + v) / L_g L_f^{\rho-1} h(x).$$

The controller reduces the input-output map to $y^{(\rho)} = v$, which is a chain of ρ integrators. In this case, the integer ρ is called the relative degree of the system.

Definition 3.1: The nonlinear system is said to have relative degree ρ, $1 \le \rho \le n$, in a region $D_0 \subset D$ if

$$L_g L_f^i h(x) = 0, \quad i = 0,\ldots \rho - 2$$
$$L_g L_f^i h(x) \ne 0, \quad i = \rho - 1$$

for all $x \in D_0$. The feedback linearized system can be formulated as

$$\begin{cases} \dot{\xi} = A\xi + Bv, \\ y = C\xi, \end{cases} \quad (4)$$

where

$$\xi = \begin{pmatrix} h \\ L_f h \\ \vdots \\ L_f^{\rho-2} h \\ L_f^{\rho-1} h \end{pmatrix}, A = \begin{pmatrix} 0 & 1 & 0 & \cdots & 0 \\ 0 & 0 & 1 & \ddots & \vdots \\ \vdots & \vdots & \ddots & \ddots & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix}, B = \begin{pmatrix} 0 \\ 0 \\ \vdots \\ 0 \\ 1 \end{pmatrix}, C = \begin{pmatrix} 1 \\ 0 \\ \vdots \\ 0 \\ 0 \end{pmatrix}^T.$$

□

The stabilizing linear controller $v = -F\xi$ of the linearized system (4) can be obtained so that the transfer function $G = C(sI - A)^{-1} B$ is Hurwitz. Due to lack of space, this paper only deals with the case of $\rho = n$.

IV. Observer Linearization

We consider the nonlinear system (1). If there exists a coordinate transformation $\zeta = \phi(x)$ such that the system (1) can be transformed into the following system:

$$\dot{\zeta} = A_0 \zeta + k(y) + r(y)u$$
$$y = C_0 \zeta$$

with (C_0, A_0) observable and $k, r : \Re \to \Re^n$ then it would be possible to build a full order state observer:

$$\dot{\hat{\zeta}} = A_0\hat{\zeta} + k(y) + H(\hat{y} - y)$$
$$\hat{y} = C_0\hat{\zeta}$$

The estimation error $e = \hat{\zeta} - \zeta$ satisfies the linear differential equation: $\dot{e} = (A_0 + HC_0)e$. The estimation state is $\hat{x} = \phi^{-1}(\hat{\zeta})$. This problem is referred to as the observer linearization problem. The following theorem [13] gives a necessary and sufficient condition for the solution of the observer linearization problem.

Theorem 4.1: The observer linearization problem [13] is solvable if and only if there exists the neighborhood V of an initial condition x_0 satisfies the following two conditions.

C1: $\dim(\text{span}\{dh(x),\ldots dL_f^{n-1}h(x)\}) = n$, where $\forall x \in V$.

C2: $[ad_f^i\tau(x), ad_f^j\tau(x)] = 0$, where $0 \le i \le n-1$, $0 \le j \le n-1$, $x \in V$.

The vector field $\tau(x)$ satisfies

$$(dh(x)^T, dL_f h(x)^T,\ldots,dL_f^{n-1}h(x)^T)^T \tau(x) = (0,\ldots,0,1)^T$$

$\square$

If the nonlinear system (1) is observer linearizable there exists a coordinate transformation $\zeta = \phi(x)$ satisfies the following condition.

$$L_{(-1)^{j-1}ad_f^{j-1}\tau}\phi_i(x) = \begin{cases} 0, & i \ne j \\ 1, & i = j \end{cases} \quad (5)$$

The coordinate transformation ζ can be constructed as

$$\zeta = \phi(x) = (\phi_1(x),\phi_2(x),\ldots,\phi_n(x))^T$$

V. TORA System

We consider TORA (Translational Oscillator with Rotating Actuator) system [14] which is one of the benchmark problem for nonlinear control. A coordinate transformation is applied to TORA system (Fig. 2) then the dynamics [14] is represented as

$$\begin{cases} \dot{x} = f(x) + gu = \begin{pmatrix} x_2 \\ -x_1 + \varepsilon\sin x_3 \\ x_4 \\ 0 \end{pmatrix} + \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix}u \\ y = h(x) = x_1 \end{cases} \quad (6)$$

where $x \in \mathfrak{R}^4$, $y \in \mathfrak{R}$, and the parameter ε depends on the eccentricity, cart mass, and ball mass. In this paper, we apply the proposed methods to TORA system (6).

Figure 2: TORA system
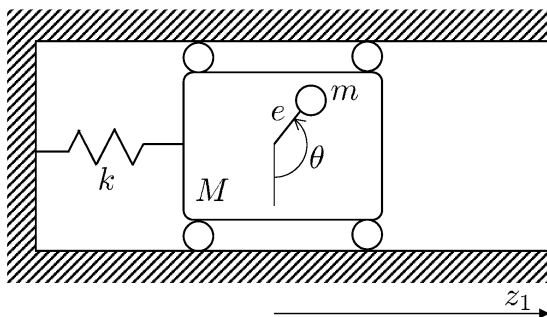
VI. PML Model of TORA System

We construct the PML model of TORA system (6). The state variable x is divided by $m_1 \times m_2 \times m_3 \times m_4$ vertices,

$$x_1 \in \{d_1(1),\ldots,d_1(m_1)\}, \quad x_2 \in \{d_2(1),\ldots,d_2(m_2)\},$$
$$x_3 \in \{d_3(1),\ldots,d_3(m_3)\}, \quad x_4 \in \{d_4(1),\ldots,d_4(m_4)\}.$$

The PML model is expressed as (2), where $x \in R_{\sigma_1\ldots\sigma_4}$,

$$f_p(x) = \sum_{i_1=\sigma_1}^{\sigma_1+1}\cdots\sum_{i_4=\sigma_4}^{\sigma_4+1} \omega_1^{i_1}(x_1)\cdots\omega_4^{i_4}(x_4)\begin{pmatrix} d_2(i_2) \\ -d_1(i_1) + \varepsilon\sin d_3(i_3) \\ d_4(i_4) \\ 0 \end{pmatrix},$$

$$g_p = \begin{pmatrix} 0 & 0 & 0 & 1 \end{pmatrix}^T,$$

$$\omega_j^{\sigma_j}(x_j) = (d_j(\sigma_j+1) - x_j)/(d_j(\sigma_j+1) - d_j(\sigma_j)),$$

$$\omega_j^{\sigma_j+1}(x_j) = (x_j - d_j(\sigma_j))/(d_j(\sigma_j+1) - d_j(\sigma_j)), j=1,\ldots,4.$$

The model is found to be fully parametric and the internal model dynamics is described by multi-linear interpolation of the vertices: $d_1(i_1)$, $d_2(i_2)$, $d_3(i_3)$ and $d_4(i_4)$ (see Fig. 1).

Note that there are some modeling errors because the PML model is a nonlinear approximation. In proposed method the vertices $d_j(i_j)$ of an arbitrary number can be set on arbitrary position of the state space. Therefore it is easily possible to adjust the approximated error.

VII. Controller Designs for TORA System

A. Exact Feedback Linearization of Original Nonlinear Systems

We design the controller of TORA system (6) via the exact feedback linearization [13]. The time derivatives of the output y have to be calculated until the input u appears. Then the controller is obtained as

$$u = \frac{-x_1 + \varepsilon\sin x_3 + \varepsilon x_4^2\sin x_3}{\varepsilon\cos x_3} + \frac{1}{\varepsilon\cos x_3}v \quad (7)$$

where v is the linear controller for the following linearized system (4), where $\xi = (h, L_f h, L_f^2 h, L_f^3 h)^T$. The parameters A, B, and C are the same as the system (4).

However, the controller (7) is only well defined at $-\pi/2 < x_3 < \pi/2$ because the denominator of the controller is $\varepsilon\cos x_3$. Hence the rotor x_3 of TORA system can only be rotated at $-\pi/2 < x_3 < \pi/2$.

B. Exact Feedback Linearization of PML Systems

We design the controller via the exact feedback linearization using the PML model (2) of TORA system. The time derivatives of the output y also have to be

calculated until the input u appears. Then the controller is obtained as

$$u = (-L_{f_p}^4 h_p + v) / L_{g_p} L_{f_p}^3 h_p u$$

$$= \frac{\sum_{i_1=\sigma_1}^{\sigma_1+1} \sum_{i_3=\sigma_3}^{\sigma_3+1} \omega_1^{i_1}(x_1) \omega_3^{i_3}(x_3)(-d_1(i_1) + \varepsilon \sin d_3(i_3))}{\varepsilon(\sin d_3(i_3+1) - \sin d_3(i_3)) / (d_3(i_3+1) - d_3(i_3))}$$
$$- \frac{d_3(i_3+1) - d_3(i_3)}{\varepsilon(\sin d_3(i_3+1) - \sin d_3(i_3))} v$$
(8)

where $v = -F\xi$ is the linear controller of the linear system (4), where $\xi = (h, L_f h, L_f^2 h, L_f^3 h)^T$. The parameters A, B, and C are the same as the system (4). If $\sin d_3(i_3+1) \neq \sin d_3(i_3)$, $i_3 = 1,...,m_3$, there exists a PML controller (8) of TORA system (6) at $\forall x_3$ since $L_{g_p} L_{f_p}^3 h_p \neq 0$. Thus we have to construct the PML model of TORA system such that $\sin d_3(i_3+1) \neq \sin d_3(i_3)$. Therefore the PML model based controller (8) can be applied to a wider region than the conventional feedback linearized controller (7).

VIII. Observer Designs for TORA System

A. Exact Observer Linearization of Original Nonlinear System

C1 of Theorem 4.1 is calculated for the original nonlinear system (6).

$$\det D_1 = \varepsilon^2 \cos^2 x_3 ,$$

where $D_1 = (dh(x)^T dL_f h(x)^T,...,dL_f^{n-1} h(x)^T)^T$. The matrix D_1 is not linear independence at $x_3 = \pm \pi/2$. One of the condition C2 is also calculated for the original nonlinear model as follows:

$$[ad_f^0 \tau(x), ad_f^3 \tau(x)] = \frac{2 \sin x_3}{\varepsilon^2 \cos^3 x_3}$$

The above equation is equal to 0 at $x_3 = 0$ and the equation cannot be defined at $x_3 = \pm\pi/2$. Therefore the nonlinear system (6) is not observer linearizable.

B. Exact Observer Linearization of PML System

C1 of Theorem 4.1 is calculated for the PML system (2) of TORA system (6).

$$\det(dh(x)^T dL_f h(x)^T,...,dL_f^{n-1} h(x)^T)^T = a \neq 0 ,$$

where a is a non-negative constant value. C2 of Theorem 4.1 is also calculated for the PML model (2) of TORA system (6).

$$[ad_f^i \tau(x), ad_f^j \tau(x)] = 0,$$

where $0 \leq i \leq 3$, $0 \leq j \leq 3$ and $\tau(x) = (0 \quad 0 \quad 0 \quad 1/a)^T$. Therefore the PML system (3) is observer linearizable. From the conditions (5), the coordinate transformation vector $\zeta = \phi(x) = (ax_4 \quad ax_3 \quad x_2 \quad x_1)^T$ can be constructed. We

can also design the observer gain H such that the estimation error system $\dot{e} = (A_0 + HC_0)e$ is stable.

IX. Simulation result

We design the PML model based linearized controller (8) and the observer for TORA system (6) in a computer simulation. In this simulation, the state variables x_1, x_2, x_3, and x_4 of TORA system are divided by the following vertices.

$$x_1 \in \{-2.5, 0, 2.5\} , \quad x_2 \in \{-2.5, 0, 2.5\}$$
$$x_3 \in \{-\pi, -7\pi/8, ..., \pi\}, \quad x_4 \in \{-10, 0, 10\}$$

The parameter ε is 0.5. The control system parameters are as follows: the feedback gain is $F = (1.000 \quad 3.078 \quad 4.236 \quad 3.078)$, the observer gain is $H = (316.2 \quad 764.4 \quad 765.9 \quad 318.6)^T$, and the observer system matrices are

$$A_0 = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}, C_0 = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 1 \end{pmatrix}^T .$$

The initial conditions are $x(0) = (1 \quad 0 \quad 0 \quad 0)^T$ and $\zeta(0) = (0 \quad 0 \quad 0 \quad 0)^T$. Figs. 3 and 4 show the linearized observer states and the estimated states. Fig. 5 shows the state responses.
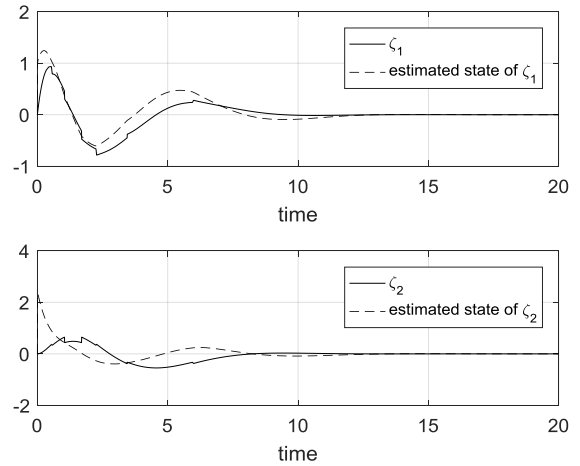

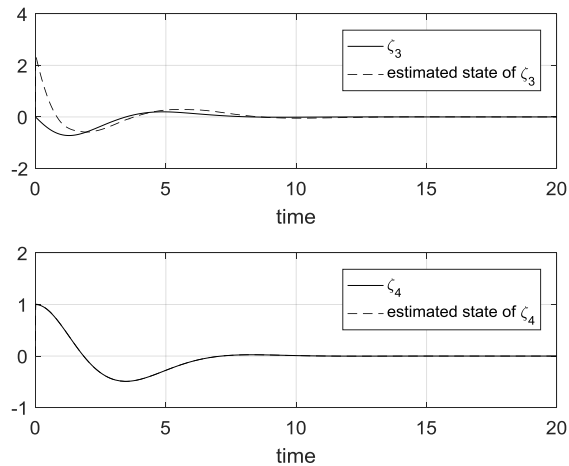Figure 3: Linearized observer states (ζ_1, ζ_2) and the estimations of TORA system

Figure 4: Linearized observer states (ζ_3 , ζ_4) and the estimations of TORA system
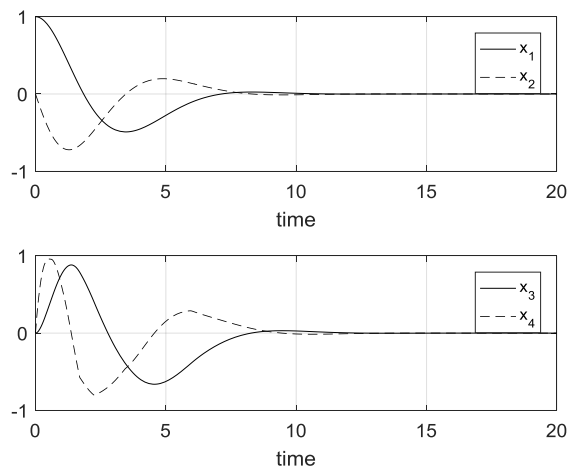

Figure 5: State responses of TORA system

x. **Conclusion**

This paper has proposed an observer design for piecewise nonlinear systems via observer linearization. The model is a PML system, a nonlinear approximation, and fully parametric. Feedback linearization can be applied to stabilize PML control systems. However, since exact observer linearized conditions are more conservative than exact feedback linearized ones, the exact observer linearization can be applied to only a few nonlinear systems. This paper has showed the PML model based linearized observer could be applied to a wider system than the conventional one. We have applied the proposed method to TORA system which was one of the benchmark problem for nonlinear control. Example has been shown to confirm the feasibility of our proposals by computer simulation.

In future work, we will apply the proposed methods to real systems and will design an observer-based feedback controller for nonlinear systems using PML models.

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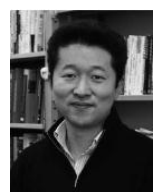
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