

METHOD N2 – ACCORDING TO FAJFAR

Arton Dautaj, Naser Kabashi and Hajdar Sadiku

Abstract: A relatively simple nonlinear method for the seismic performance evaluation of structures (the N2 method) is presented. The method combines the nonlinear static (pushover) analysis and the response spectrum approach. The method yields results of reasonable accuracy if the structure oscillates predominantly in the first mode. In the paper the method is formulated in the acceleration – displacement format. This versions combine the advantages of the visual representation of CSM developed by Freeman. By reversing the analysis process, the method can be used as a tool for the implementation of the direct displacement-based design approach.

Keywords: "Pushover analysis", performance evaluation, inelastic behavior, ductility etc.

Introduction

For the rational design of buildings from seismic operations, design methods must meet the following requirements:

- a) adequately respond to requests of stiffness, strength and ductility during an expected earthquake[5], and
- b) not be complicated[5].

The methods applied in the various codes (analysis of equivalent lateral force and modal spectral analysis) are based on the assumption of linear elastic behavior of the structure and as such, regardless of the application to them of various modifier and corrective factors, fail to satisfy the first request adequately.

On the other hand, nonlinear dynamical analysis of the system with many degrees of freedom is relatively complicated and, as such, are not very suitable for everyday design.

Method N2 (N2 designation relates to the fact that it requires the application of a nonlinear method - "Nonlinear" - and the construction of two models) meets the two requirements above

N2 method in Europe is developed in Slovenia, in the University of Ljubljana and is based on the so-called model-Q, filed by Saiidi and Sozen [23] for simple nonlinear analysis of systems with multi degrees of freedom. Later, this method has been developed through different stages and for different systems, while now has been included in the final draft of the EC 8 [3]

N2 method provides results with sufficient accuracy and can be used for systems where seismic response is dominated by the contribution of the first form of vibration.

Initially N2 method is presented for "regular" systems (Fajfar & Fischinger, 1987 ECEE [4], 1989 WCEE [5]). As basic proposals of this method are the use of two different mathematical models and the application of three main steps in the analysis. In the first step is determined the stiffness (rigidity), strength and ductility. For this applies nonlinear static analysis of the system with many degrees of freedom (MDOF) by the action of a form of distribution of loads that monotonically increasing.

In the second step is defined equivalent system with single degree of freedom. Nonlinear characteristics of equivalent system are based on the relation base shear force -displacement on the roof designated by nonlinear static analysis in the first step. While on the third step of the method N2 from nonlinear dynamic analysis of the equivalent system with single degree of freedom is determined the maximum displacement (and corresponding demand on ductility). The third step, in a simple form can be performed using inelastic spectra.

As mentioned above, the use of inelastic spectra in the third step can simplify a lot the analysis and make it highly suitable for daily practice project.

After processing of the first ideas, the method has already found numerous applications of seismic analysis and anti-seismic design (reinforced concrete buildings considering the remaining damages, according Fajfar and Gaspersic [16], bridges, asymmetric buildings; spatial buildings; and, finally assessment of performance). Actually, the N2 method is formulated in the format AD [14,17], acceleration-displacement.

Arton Dautaj¹

Naser Kabashi¹

Hajdar Sadiku¹

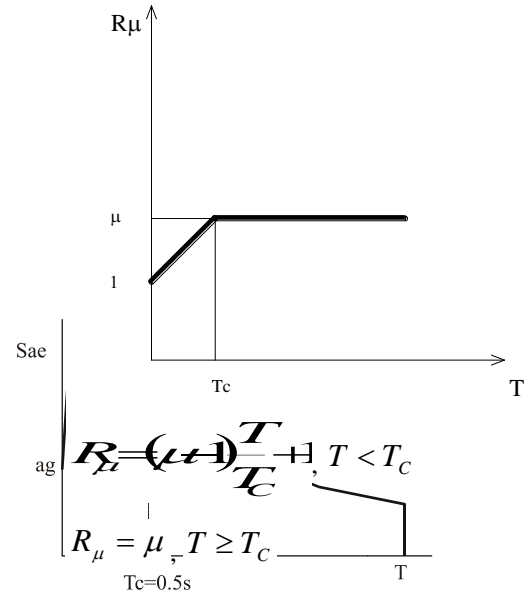
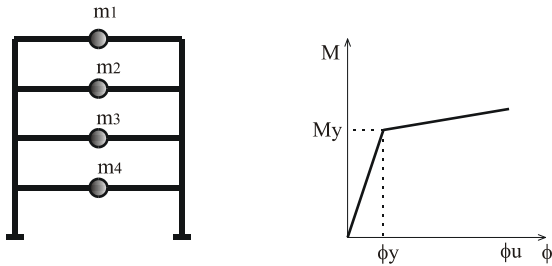
¹Civil Engineering and Architectural Faculty, University "Hasan Prishtina" of Prishtina
Republic Of Kosova,

The following is given recently developed version of the method N2.

1. Summary of N2 method

I. Data

- Structure
- Moment-curved geometry relationship
- Elastic spectra of accelerations



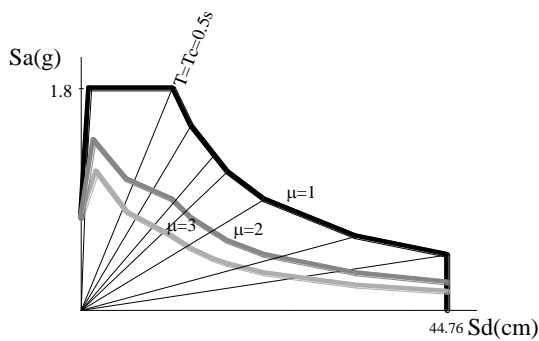
II. Seismic demands on format AD

- Define elastic spectra in AD format

$$S_{de} = \frac{T^2}{4T_c^2} S_{ae}$$

- Define the inelastic spectra for constant ductility

$$S_a = \frac{S_{ae}}{R_\mu}, S_d = \frac{\mu}{R_\mu} S_{de}$$

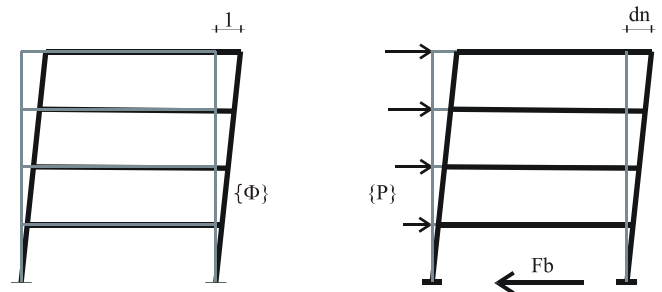


III. "Pushover" analysis

- Assume the form of displacement $\{\Phi\}$
- Determine the vertical distribution of lateral force

$$\{P\} = [M]\{\Phi\}, P_i = p n_i \Phi_i$$

- Define the relationship "based shear force - displacement on the roof".



IV. Equivalent model with single degree of freedom.

- Define the mass m^*

$$m^* = \sum_{i=1}^n m_i \Phi_i^2$$

- Transform quantities (Q) of system with multi degrees of freedom in quantities (Q^*) of the system with single degree of freedom

$$Q^* = \frac{Q}{\Gamma}, \quad \Gamma = \frac{m^*}{\sum_{i=1}^n m_i \Phi_i^2}$$

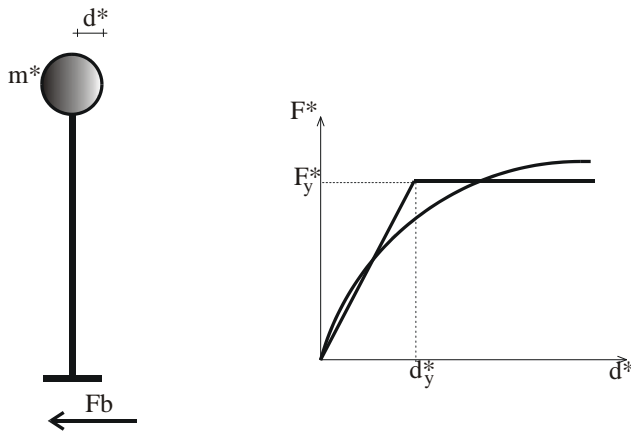
c) Determine the approximate relationship elastic-plastic force-displacement

d) Determine the strength F_y^* , yield displacement d_y^* and period T^* .

$$T^* = 2\pi \sqrt{\frac{m^* d_y^*}{F_y^*}}, \quad (k^* = F_y^*/d_y^*)$$

e) Determine the diagram of capacity (acceleration versus displacement)

$$S_a = \frac{F^*}{m^*}$$



V. Seismic demand for the model with single degree of freedom.

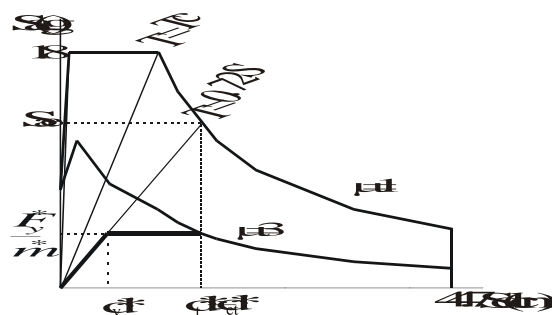
a) Define reducing factor R_μ

$$R_\mu = \frac{S_{ae}}{S_{ay}}$$

b) Define displacement demand

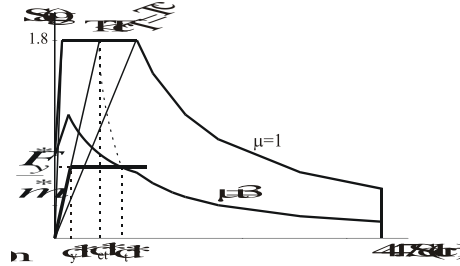
$$d^* = S_d = S_{de} \left(\frac{T^*}{T_c} \right)^{\alpha}, \quad T^* < T_c$$

$$d^* = S_d = S_{de}, \quad T^* \geq T_c$$

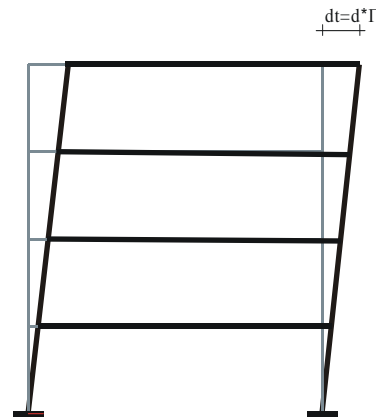


VI. Global seismic demand for the model with many degrees of freedom.

a) Transform the displacement demand of the system with single degree of freedom to the top displacement of multi degrees of freedom model.



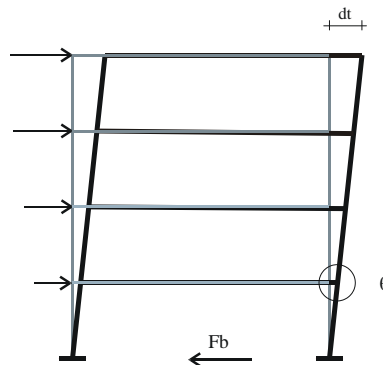
$$d_t = \Gamma d^*$$



VII. Local seismic demand

a) Apply the analysis "pushover" in the model with multi degrees of freedom (MDOF) until reaching the displacement in d_t

b) Determine local quantities (relative displacement of floors, rotation of joints etc.), corresponding to d_t



VIII. Performance Assessment

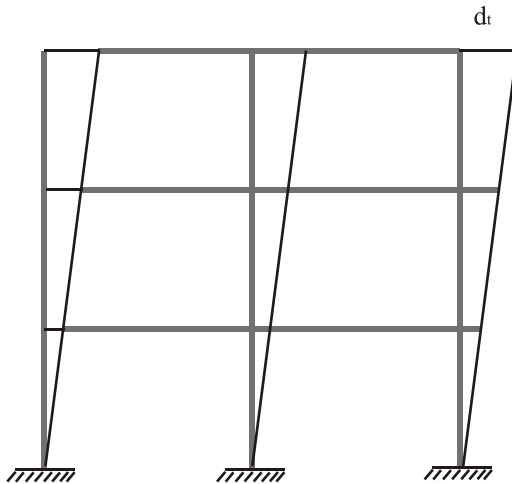
a) Compare local and global seismic demand with capacity to the required level of performance.

2. APPLICATION OF THE METHOD N2 IN DESIGN

With the inversion of procedure of method N2 used for assessment of the performance, can be developed a design methodology based directly on the displacement. Practically will be done this way:

1st Step.

For the required performance (defined) is given the displacement $d_{t(n)}$, which represents the displacement on the roof of the system with many degrees of freedom.



2nd Step.

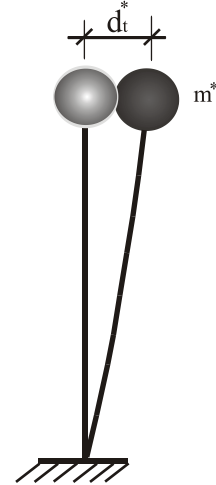
Determining the displacement of the system with single degree of freedom

$$d_t^* = S_d^* = \frac{d_t}{\Gamma}$$

where $\Gamma \cong \frac{3n}{2n+1}$ or $\Gamma = \frac{m^*}{\sum_{i=1}^n m_i \Phi_i^2}$, where n-

number of floors, $m^* = \sum_{i=1}^n m_i \Phi_i^2$

Φ_i - linear form of vibration (first form of vibration).



3rd Step.

Determining the ductility or stiffness (rigidity) of the structure. To define the ductility, initially should be determined the yield displacement for the system.

$$d_{yt}^* = \frac{d_{yt}}{\Gamma}$$

Ductility will be

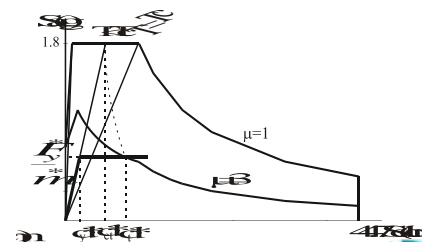
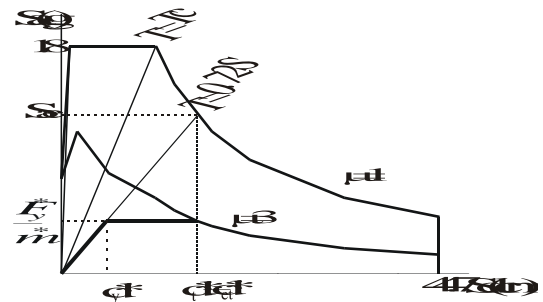
$$\mu = \frac{d_t^*}{d_{yt}^*}$$

4th Step.

For the defined quantity d_t^* appreciate S_{ae} and T^* . Further apply the following expressions:

$$R_\mu = \mu \text{ per } T^* \geq T_C,$$

$$R_\mu = (\mu - 1) \frac{T^*}{T_C} + 1 \text{ per } T^* < T_C$$



$$S_{ay} = \frac{S_{ae}}{R_{\mu}}$$

Thus, base shear force of the system with single degree of freedom will be:

$$S_{ay} = \frac{F_y^*}{m} = F_y^*$$

5th Step.

Determine the base shear force for the system with multi degree of freedom.

$$F_b = F_y^* \cdot \Gamma$$

6th Step.

The distribution in the height of the structure of horizontal load adapting assumed displacement profile:

$$F_i = \frac{\Phi_i m_i}{\sum_{i=1}^n \Phi_i m_i} F_b$$

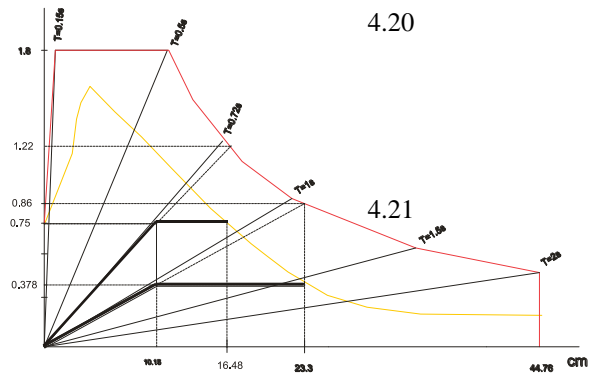


Fig.1. Displacement demand for ag=0.6g, B, EC8, v.2002

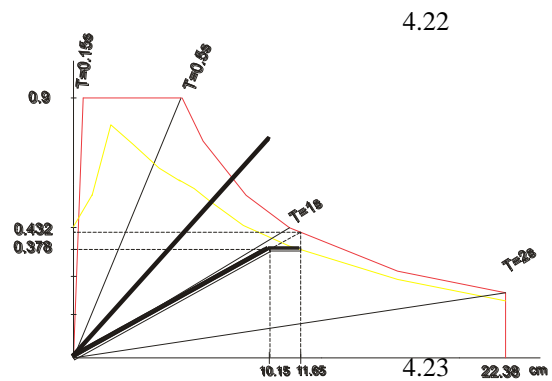
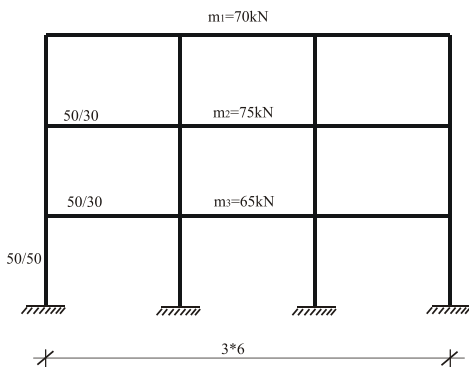


Fig.2. Displacement demand for 0.3g, B, EC8, v.2002

For four cases of seismic demand, the results are presented below in tabular form.

Example:

According to the Fajfar method N2 to evaluate the structure for seismic demand by EC-8, B, ag=0.3g, 0.4g, 0.5g and 0.6g



From the "pushover" analysis is defined the relationship base shear force – displacement on the roof.

$$F_b = 670 \text{ kN}, d_{yt} \cong 13 \text{ cm}$$

	0.3g	0.4g	0.5g	0.6g
F_b (kN)	670	670	670	670
d_{yt} (cm)	13	13	13	13
m^* (ton)	141	141	141	141
F_y^* (kN)	523	523	523	523
d_{yt}^* (cm)	10.15	10.15	10.15	10.15
T^* (s)	1.04	1.04	1.04	1.04
k^* (kN/m)	5153.8	5153.8	5153.8	5153.8
S_{ay} (m/s^2)	0.378g	0.378g	0.378g	0.378g
S_{ae} (m/s^2)	0.432g	0.57g	0.72	0.86
R_{μ}	1.14	1.53	1.91	2.29
d_t^* (cm)	11.65	15.53	19.42	23.3
d_t (cm)	14.93	19.91	24.89	29.86

According to the DDBD N2method - Fajfar,

For the defined performance $d_{(r)} = 15\text{ cm}$ and seismic demand, $a_g = 0.3g, 0.4g, 0.5g$ and $0.6g$ to be determined the base shear force

$$\Gamma = 1.28$$

$$m^* = 141\text{ ton}$$

$$d_t^* = 15\text{ cm}$$

$$d_{yt}^* = 13\text{ cm}$$

$$\mu = 1.15$$

$$S_{ae} = 0.43g$$

$$T^* = 1.04$$

From the design spectra can be obtained (read):

$$S_{ae} = 0.43g \text{ dhe } T^* = 1.04$$

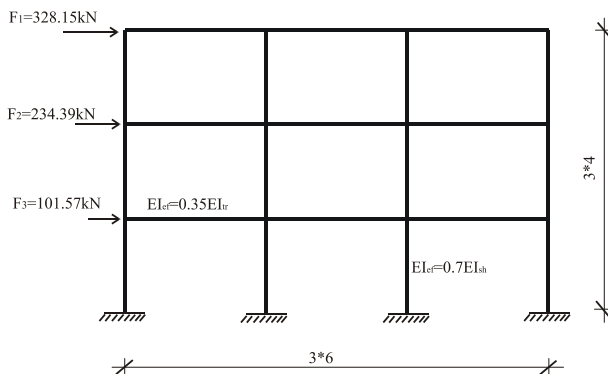
$$S_{ay} = \frac{S_{ae}}{R_\mu} = 0.37g, F_y^* = 518.28$$

$$F_b = 664.12\text{ kN}$$

$$F_1 = 328.15\text{ kN}$$

$$F_2 = 234.39\text{ kN}$$

$$F_3 = 101.57\text{ kN}$$



For four cases of seismic demand, the results are presented below in tabular form

	0.3g	0.4g	0.5g	0.6g
m^* (ton)	141	141	141	141
Γ	1.28	1.28	1.28	1.28
d_t (cm)	15	15	15	15
d_t^* (cm)	11.71	11.71	11.71	11.71
d_{yt} (cm)	13	13	13	13
d_{yt}^* (cm)	10.15	10.15	10.15	10.15
μ	1.15	1.15	1.15	1.15
S_{ae} (m/s^2)	0.43g	0.76g	1.195	1.49g
T^* (s)	1.04	0.78	0.627	0.52
R_μ	1.15	1.15	1.15	1.15
S_{ay} (m/s^2)	0.37g	0.66g	1.035g	1.49g
F_y^* (kN)	518.28	921.37	1439.64	2073.09
F_b (kN)	664.12	1180.65	1844.78	2656.48

Conclusion

N2 method can be used both for the seismic performance evaluation of newly designed or existing structures. Furthermore, by reversing the analysis process, the method can be used as a tool for the implementation of direct displacement-based design approach, in which design starts from a predetermined target displacement. The limitations of the methods based on pushover analysis should be recognized. A detailed discussion of pushover analysis can be found in (Krawinkler and Seneviratna)

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